

DL usuels

$e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \cdots + \frac{x^n}{n!} + o_{x \rightarrow 0}(x^n) = \sum_{k=0}^n \frac{x^k}{k!} + o_{x \rightarrow 0}(x^n)$
$\text{ch}(x) = 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \cdots + \frac{x^{2n}}{(2n)!} + o_{x \rightarrow 0}(x^{2n+1}) = \sum_{k=0}^n \frac{x^{2k}}{(2k)!} + o_{x \rightarrow 0}(x^{2n+1})$
$\text{sh}(x) = x + \frac{x^3}{3!} + \frac{x^5}{5!} + \cdots + \frac{x^{2n+1}}{(2n+1)!} + o_{x \rightarrow 0}(x^{2n+2}) = \sum_{k=0}^n \frac{x^{2k+1}}{(2k+1)!} + o_{x \rightarrow 0}(x^{2n+2})$
$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} + \cdots + (-1)^n \frac{x^{2n}}{(2n)!} + o_{x \rightarrow 0}(x^{2n+1}) = \sum_{k=0}^n (-1)^k \frac{x^{2k}}{(2k)!} + o_{x \rightarrow 0}(x^{2n+1})$
$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} + \cdots + (-1)^n \frac{x^{2n+1}}{(2n+1)!} + o_{x \rightarrow 0}(x^{2n+2}) = \sum_{k=0}^n (-1)^k \frac{x^{2k+1}}{(2k+1)!} + o_{x \rightarrow 0}(x^{2n+2})$
$\tan(x) = x + \frac{x^3}{3} + o_{x \rightarrow 0}(x^3)$
$(1+x)^\alpha = 1 + \alpha x + \cdots + \frac{\alpha(\alpha-1)\cdots(\alpha-n+1)}{n!} x^n + o_{x \rightarrow 0}(x^n)$
$= \sum_{k=0}^n \frac{\alpha(\alpha-1)\cdots(\alpha-k+1)}{k!} x^k + o_{x \rightarrow 0}(x^n)$
$\frac{1}{1-x} = 1 + x + x^2 + \cdots + x^n + o_{x \rightarrow 0}(x^n) = \sum_{k=0}^n x^k + o_{x \rightarrow 0}(x^n)$
$\frac{1}{1+x} = 1 - x + x^2 + \cdots + (-1)^n x^n + o_{x \rightarrow 0}(x^n) = \sum_{k=0}^n (-1)^k x^k + o_{x \rightarrow 0}(x^n)$
$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} + \cdots + (-1)^{n-1} \frac{x^n}{n} + o_{x \rightarrow 0}(x^n) = \sum_{k=0}^n (-1)^{k-1} \frac{x^k}{k} + o_{x \rightarrow 0}(x^n)$
$\arctan(x) = x - \frac{x^3}{3} + \frac{x^5}{5} + \cdots + (-1)^n \frac{x^{2n+1}}{(2n+1)} + o_{x \rightarrow 0}(x^{2n+2}) = \sum_{k=0}^n (-1)^k \frac{x^{2k+1}}{(2k+1)} + o_{x \rightarrow 0}(x^{2n+2})$